

Estimation of Flexibility Potentials in Active Distribution Networks

Von der Fakultät
Informatik, Elektrotechnik und Informationstechnik
der Universität Stuttgart
zur Erlangung der Würde eines Doktor-Ingenieurs (Dr.-Ing.)
genehmigte Abhandlung

vorgelegt von

Daniel Alfonso Contreras Schneider

aus Santiago, Chile

Hauptberichter:	Prof. Dr.-Ing. habil. K. Rudion
Mitberichter:	Prof. Dr.-Ing. J. Myrzik
Tag der Prüfung:	04.10.2021

Institut für Energieübertragung und Hochspannungstechnik
der Universität Stuttgart

Bibliografische Information der Deutschen Nationalbibliothek:
Die Deutsche Nationalbibliothek verzeichnet diese Publikation in der Deutschen
Nationalbibliografie, detaillierte bibliografische Daten sind im Internet über
<http://dnb.dnb.de> abrufbar.

Universität Stuttgart
Institut für Energieübertragung und Hochspannungstechnik, Band 34
D 93 (Dissertation Universität Stuttgart)

Estimation of Flexibility Potentials in Active Distribution Networks

© 2021 Contreras Schneider, Daniel Alfonso

Herstellung und Verlag: BoD – Books on Demand, Norderstedt

ISBN: 978-3-75439-704-6

Abstract

Replacing conventional power plants by distributed energy resources (DER) in the MV and LV grids poses great new challenges for the planning and operation of distribution grids. Controlling a handful of conventional power plants demands significantly less resources than operating numerous decentralized plants, especially when it involves the supply of ancillary services to maintain the grid stability. Nevertheless, most ancillary services are required at the transmission system level, meaning that vertical supply of flexibility becomes necessary, requiring new methods to quantify how much flexibility can be provided from distribution (DSO) to transmission system operators (TSO). The feasible operation region (FOR) allows capturing the aggregated flexibility potential of DER within a distribution grid, while respecting the technical restrictions of both plants and grid.

This thesis proposes a novel approach to compute the FOR, the Linear Flexibility Aggregation (LFA) method, based on the solution of linear OPF. With the objective of reducing the computation time, without compromising the accuracy of the assessed FOR.

The LFA algorithm is comprehensively evaluated throughout this thesis, focusing on the accuracy and speed of the approach. The analysis quantifies the impact of the linear OPF model in the FOR computation, as well as it identifies all relevant parameters that can have an impact in the computation time.

It is shown that the proposed method provides a considerable reduction in processing time compared to similar methods, e.g. Monte-Carlo simulations or non-linear OPF-based methods. The linearization of the power flow equations has an impact in the accuracy of the solution, however, the trade-off with the reduction of the computational time is acceptable.

The dissertation closes with the suggestion of three use cases for the LFA method. Firstly, it is described how a fast computation of the FOR could be used to study the long-term provision of flexibility in distribution grids. Secondly, the usage of the LFA for the vertical aggregation of flexibility over different voltage levels is shown. Finally, the inclusion of the FOR concept in a congestion management approach, including redispatch at the distribution grid level is demonstrated. The proposal and analysis of these use cases applied to large distribution grids would not have been possible without a fast and reliable computation algorithm, like the LFA.

Overall, the coordination between grid operators can benefit significantly from the fast computation of the FOR, allowing its inclusion not only in planning processes, but also in everyday operation processes.

Table of Contents

1	Introduction	1
1.1	Motivation and Background.....	1
1.2	State-of-the-Art and Objectives.....	3
1.3	Structure of the Thesis.....	4
1.4	Scientific Thesis	5
2	Use of Flexibilities for the Provision of Ancillary Services in Power Systems	6
2.1	Flexibility in Power Systems.....	6
2.2	Flexibility Providing Units (FPU).....	10
2.3	Vertical Provision of Flexibility for Ancillary Services	13
2.4	Capability Charts of FPU.....	15
2.4.1	Definition of Reference Convention.....	15
2.4.2	Capability Charts of Different Types of DER	16
2.4.3	Grid Codes Requirements.....	25
3	Feasible Operation Region of Active Distribution Networks	27
3.1	Feasible Operating Region (FOR)	28
3.2	Approaches to Compute the FOR of Distribution Grids.....	30
3.2.1	Analytic Approaches	30
3.2.2	Geometric Approaches.....	33
3.2.3	Random Sampling Approaches.....	34
3.2.4	Optimization Based Approaches	40
4	Fast Computation of FOR with Linear Optimization	48
4.1	Method Objectives and Differentiation	48
4.2	Linear OPF-based Method to Compute the FOR.....	49
4.2.1	General Formulation of a Linear OPF	50
4.2.2	Linearization of Power Flow Equations	50
4.2.3	Adding FPU Flexibility into State Variables Vector	53
4.2.4	Linearization of Branch Flow Equations	54
4.2.5	Voltage and Branch Flow Constraints	54
4.2.6	FPU/FPG Constraints.....	56
4.2.7	Objective Function	57
4.2.8	Selection of Initial Operation Point	58
4.2.9	Iterative Reconstruction of FOR boundaries	58
4.2.10	On the Convexity of the FOR	60
4.2.11	Method to Correct Linearization Error in FOR.....	61
4.3	Modelling of Linear FPU/FPG Boundaries	62

4.4	Impact of Topology Changes on FOR Computation.....	65
4.4.1	Switching Power Lines	65
4.4.2	OLTC Transformers.....	67
4.5	Coupling the Linear Aggregation Method with Time-Series	67
4.5.1	Modelling of FPU Considering Time-Series.....	68
4.5.2	Sequential FOR Computation Using Time-Series	70
5	Validation of Linear Flexibility Aggregation Method.....	72
5.1	Grid Models	72
5.1.1	CIGRE MV Grid	72
5.1.2	CIGRE LV Feeders.....	73
5.1.3	Real Urban Distribution Grid.....	73
5.2	Validation of Linear Power Flow Model	75
5.3	FOR Linearization Error Correction in LFA.....	77
5.4	Analysis of the Convexity of the FOR Computation.....	80
5.5	Impact of Grid Topology and Constraints in the FOR.....	83
5.6	Comparison Between LFA and RS Approaches	86
5.7	Comparison of LFA to Similar Approaches	91
6	Use Cases for the Planning and Operation of Distribution Grids	94
6.1	Time-Series Based Aggregation.....	95
6.1.1	Long-Term Time-Series Analysis	96
6.1.2	Short-Term Time-Series-based Analysis.....	100
6.2	Multi-Level Aggregation.....	104
6.2.1	Multi-Level Aggregation in MV/LV Grids.....	106
6.2.2	Impact of Voltage at the Interconnection Point.....	107
6.2.3	Voltage Correction at Interconnection Points	110
6.2.4	Multi-Level Aggregation in HV/MV Grids	111
6.3	Redispatch Concept.....	115
6.3.1	Definition of redispatch OPF including FOR constraints.....	116
6.3.2	Operating a redispatch concept using FOR.....	117
6.3.3	Numerical Results	117
7	Conclusion and Outlook.....	120
7.1	Conclusion	120
7.2	Outlook.....	122
8	References.....	124
	Appendix.....	140

8 References

- [1] J. Cohn, "When the Grid Was the Grid: The History of North America's Brief Coast-to-Coast Interconnected Machine," *Proceedings of the IEEE*, vol. 107, no. 1, pp. 232-243, Jan. 2019.
- [2] S. Howell, Y. Rezgui, J.-L. Hippolyte, B. Jayan and H. Li, "Towards the Next Generation of Smart Grids: Semantic and Holonic Multiagent Management of Distributed Energy Resources," *Renewable and Sustainable Energy Reviews*, vol. 77, pp. 193-214, 2017.
- [3] R. Hidalgo, C. Abbey and G. Joós, "A Review of Active Distribution Networks Enabling Technologies," in *IEEE PES General Meeting*, Providence, RI, USA, Jul. 2010.
- [4] D. A. Contreras and K. Rudion, "Improved Assessment of the Flexibility Range of Distribution Grids Using Linear Optimization," in *Power Systems Computing Conference (PSCC)*, Dublin, Ireland, 2018.
- [5] I. Ilic, A. Viskovic and M. Vrazic, "User P-Q Diagram as a Tool in Reactive Power," in *International Conference on the European Energy Market (EEM)*, Zagreb, Croatia, May 2011.
- [6] J. R. de Silva, *Capability Charts of Power Systems*, Canterbury, New Zealand: University of Canterbury, Mar. 1987.
- [7] D. Mayorga, J. Hachenberger, J. Hinker, F. Rewald, U. Häger, C. Rehtanz and J. Myrzik, "Determination of the Time-Dependant Flexibility of Active Distribution Networks to Control Their TSO-DSO Interconnection Power Flow," in *Power Systems Computing Conference (PSCC)*, Dublin, Ireland, 2018.
- [8] A. Losi, F. Rossi, M. Russo and P. Verde, "New Tool for Reactive Power Planning," *IEE Proceedings*, vol. 140, no. 4, pp. 256-262, Jul. 1993.
- [9] E. Chiodo, A. Losi, R. Mongelluzzo and F. Rossi, "Capability Charts for Electrical Power Systems," *IEEE Proceedings-c*, vol. 189, no. 1, pp. 71-75, Jan. 1992.
- [10] S. M. Abdelkader and D. Flynn, "Graphical Determination of Network Limits for Wind Power Integration," *IET Generation, Transmission & Distribution*, vol. 3, no. 9, pp. 841-849, 2009.

- [11] P. Cuffe, P. Smith and A. Keane, "Capability Chart for Distributed Reactive Power Resources," *IEEE Transactions on Power Systems*, vol. 29, no. 1, pp. 15-22, Jan. 2014.
- [12] P. Goergens, F. Portratz, M. Gödde and A. Schnettler, "Determination of the Potential to Provide reactive Power from Distribution Grids to the Transmission Grid Using Optimal Power Flow," in *International Universities Power Engineering Conference (UPEC)*, Soke on Trent, UK, Sep. 2015.
- [13] A. V. Jayawardena, L. G. Meegahapola, D. A. Robinson and S. Perera, "Capability Chart: A New Tool for Grid-Tied Microgrid Operation," in *IEEE PES T&D Conference and Exposition*, Chicago, USA, Apr. 2014.
- [14] S. Riaz and P. Mancarella, "On Feasibility and Flexibility Operating Regions of Virtual Power Plants and TSO/DSO Interfaces," in *Powertech*, Milan, Italy, Jun. 2019.
- [15] EURELECTRIC, "Flexibility and Aggregation Requirements for their interaction in the market," January 2014.
- [16] I. Talavera, S. Stepanescu, F. Bennewitz, J. Hanson, R. Huber, F. Oechsle and H. Abele, "Vertical Reactive Power Flexibility based on Different Reactive Power Characteristics for Distributed Energy Resources," in *International ETG Congress*, Bonn, Germany, Nov. 2017.
- [17] A. Keane, E. Diskin, P. Cuffe, D. Brooks, T. Hearne and T. Fallon, "Reactive Power Support from Distributed Generation - Ireland's Demonstration Initiative," in *IEEE PES General Meeting*, San Diego, CA, USA, Jul. 2012.
- [18] P. Vermeyen and P. Lauwers, "Managing Reactive Power in MV Distribution Grids Containing Distributed Generation," in *CIGRE*, Lyon, France, Jun. 2015.
- [19] M. Tomaszewski, S. Stankovic, I. Lisse and L. Söder, "Minimization of Reactive Power Exchange at the DSO/TSO Interface: Öland Case," in *ISGT Europe*, Bucharest, Romania, Sep. 2019.
- [20] P. Cuffe, P. Smith and A. Keane, "Characterisation of the Reactive Power Capability of Diverse Distributed Generators: Toward an Optimisation Approach," in *IEEE PES General Meeting*, San Diego, CA, USA, Jul. 2012.
- [21] M. Heleno, R. Soares, J. Sumaili, R. J. Bessa, L. Seca and M. A. Matos, "Estimation of the Flexibility Range in the Transmission-Distribution Boundary," in *PowerTech*, Eindhoven, Netherlands, 2015.

- [22] J. Silva, J. Sumaili, R. Bessa, L. Seca, M. Matos, V. Miranda, M. Cajouille, B. Goncer and M. Sebastian-Viana, "Estimating the Active and Reactive Power Flexibility Area at the TSO-DSO Interface," *IEEE Transactions on Power Systems*, vol. 33, no. 5, pp. 4741-4750, Sep. 2018.
- [23] J. Silva, J. Sumaili, R. J. Bessa, L. Seca, M. Matos and V. Miranda, "The challenges of estimating the impact of distributed energy resources flexibility on the TSO/DSO boundary node operating points," *Computers and Operations Research*, vol. 96, pp. 294-304, Aug. 2018.
- [24] N. Fonseca, J. Silva, A. Silva, J. Sumaili, L. Seca, R. Bessa, J. Pereira, M. Matos, P. Matos, A. Morais, M. Caujolle and M. Sebastian-Viana, "EvolVDSO Grid Management Tools to Support TSO-DSO Cooperation," in *CIREC*, Helsinki, Finland, 2016.
- [25] M. Braun, PhD Thesis: Provision of Ancillary Services by Distributed Generators, Kassel, Germany: University of Kassel, 2008.
- [26] E. Lannoye, D. Flynn and M. O'Malley, "Evaluation of Power System Flexibility," *IEEE Transactions on Power Systems*, vol. 27, no. 2, pp. 922-931, May 2012.
- [27] R. Bärenfänger, E. Drayer, D. Daniluk, B. Otto, E. Vanet, R. Caire, T. Shamsi Abbas and B. Lisanti, "Classifying Flexibility Types in Smart Electric Distribution Grids," in *CIREC Workshop*, Helsinki, Finland, 2016.
- [28] J. Zhao, T. Zheng and E. Litvinov, "A Unified Framework for Defining and Measuring Flexibility in Power System," *IEEE Transactions on Power Systems*, vol. 31, no. 1, pp. 339-347, Jan. 2016.
- [29] A. Ulbig and G. Andersson, "Analyzing Operational Flexibility of Electric Power Systems," *International Journal of Electrical Power & Energy Systems*, vol. 72, pp. 155-164, Nov. 2015.
- [30] H. Nosair and F. Bouffard, "Flexibility Envelopes for Power System Operational Planning," *IEEE Transactions on Sustainable Energy*, vol. 6, no. 3, pp. 800-809, Jul. 2015.
- [31] North American Electric Reliability Corporation (NERC), "Flexibility Requirements and Potential Metrics for Variable Generation: Implications for System Planning Studies," NERC, Princeton, NJ, USA, Aug. 2010.
- [32] K. Heussen, S. Koch, A. Ulbig and G. Andersson, "Energy Storage in Power System Operation: The Power Nodes Modeling Framework," in

- IEEE PES Innovative Smart Grid Technologies Conference Europe (ISGT Europe)*, Gothenberg, Sweden, Oct. 2010.
- [33] T. Kornrumpf and M. Zdrallek, "Analyzing Flexibility Options with Cross-Sectoral Requirements on Distribution Level," in *IEEE PES General Meeting*, Portland, OR, USA, Aug. 2018.
- [34] A. A. Jahromi and F. Bouffard, "On the Loadability Sets of Power Systems - Part I: Characterization," *IEEE Transactions on Power Systems*, vol. 32, no. 1, pp. 137-145, Jan. 2017.
- [35] J. Su and H.-D. Chiang, "Toward Characterization of the Feasible Region of Loadability of Power Systems," in *IEEE PES General Meeting*, Atlanta, GA, USA, Aug. 2019.
- [36] M. Bucher, S. Chatzivasileiadis and G. Andersson, "Managing Flexibility in Multi-Area Power Systems," *IEEE Transactions on Power Systems*, vol. 31, no. 2, pp. 1218-1226, Mar. 2016.
- [37] M. A. Bucher, S. Delikaraoglou, K. Heussen, P. Pinson and G. Andersson, "On Quantification of Flexibility in Power Systems," in *IEEE PowerTech*, Eindhoven, Netherlands, 2015.
- [38] A. Kalantari, J. F. Restrepo and F. D. Galiana, "Security-Constrained Unit Commitment With Uncertain Wind Generation: The Loadability Set Approach," *IEEE Transactions on Power Systems*, vol. 28, no. 2, pp. 1787-1796, May 2013.
- [39] G. Petretto, M. Cantú, G. Gigliucci, F. Pilo, G. Pisano, N. Natale, G. G. Soma, M. Coppo and R. Turri, "Representative Distribution Network Models for Assessing the Role of Active Distribution Systems in Bulk Ancillary Services Markets," in *Power Systems Computation Conference (PSCC)*, Genoa, Italy, Aug. 2016.
- [40] D. Contreras and K. Rudion, "CALLIA Deliverable Task 1.1 - Part B: Simulations on Use Cases for the Usage of Flexibilities in Distribution Grids," Jul. 2018. [Online]. Available: https://callia.info/wp-content/uploads/2018/09/20180628_D1_1b_v2.pdf. [Accessed 27 02 2020].
- [41] D. Contreras, O. Laribi, M. Banka and K. Rudion, "Assessing the Flexibility Provision of Microgrids in MV Distribution Grids," in *CIGRE Workshop*, Ljubljana, 2018.

- [42] B. M. Buchholz and Z. Styczynski, *Smart Grids – Fundamentals and Technologies in Electricity Networks*, Heidelberg, Germany: Springer, 2014.
- [43] D. Bernet, L. Stefanski and M. Hiller, "A Hybrid Medium Voltage Multilevel Converter with Parallel Voltage-Source Active Filter," in *10th International Conference on Power Electronics - ECCE Asia*, Busan, Korea, May 2019.
- [44] D. Pudjianto, C. Ramsay and G. Strbac, "Virtual Power Plant and System Integration of Distributed Energy Resources," *IET Renewable Power Generation*, vol. 1, no. 1, pp. 10-16, 2007.
- [45] VDE, "VDE-AR-N 4105 - Power Generating Plants in the Low Voltage Network," VDE, Berlin, Germany, 2019.
- [46] VDE, „VDE-AR-N 4110 - Technical Connection Rules for Medium-Voltage,“ VDE, Berlin, Germany, 2019.
- [47] International Energy Agency (IEA), "Do It Locally: Local Voltage Support by Distributed Generation – A Management Summary," IEA, Germany, Jan. 2017.
- [48] M. Stötzer, P. Gronstedt, Z. Styczynski, B. M. Buchholz, W. Glaunsinger and K. V. Suslov, "Demand Side Integration - A Potential Analysis for the German Power System," in *IEEE PES General Meeting*, San Diego, CA, USA, Jul. 2012.
- [49] R. D'hulst, W. Labeeuw, B. Beusen, S. Claessens, G. Deconinck and K. Vanthournout, "Demand Response Flexibility and Flexibility Potential of Residential Smart Appliances: Experiences from Large Pilot Test in Belgium," *Applied Energy*, vol. 155, pp. 79-90, 2015.
- [50] SmartNet, "D1.1 Ancillary Service Provision by RES and DSM Connected at Distribution Level in the Future Power System," Dec. 2012.
- [51] dena, "Ancillary Services Study 2030," Berlin, Germany, Jul. 2014.
- [52] H. Gerard, E. Rivero and D. Six, "Coordination Between Transmission and Distribution System Operators in the Electricity Sector – A Conceptual Framework," *Utilities Policy*, vol. 50, pp. 40-48, 2019.
- [53] E. Rivero, D. Six, A. Ramos and M. Maenhoudt, "Deliverable 1.3 - Preliminary assessment of the future roles of DSOs, future market

- architectures and regulatory frameworks for network integration of DRES," 2014. [Online]. Available: <http://www.evolvdso.eu>.
- [54] C. Zhang, Y. Ding, N. C. Nordentoft, P. Pinson and J. Østergaard, "FLECH: A Danish Market Solution for DSO Congestion Management Through DER Flexibility Services," *Journal of Modern Power Systems and Clean Energy*, vol. 2, no. 2, pp. 126-133, 2014.
- [55] R. Schwerdfeger, PhD Thesis: Vertikaler Netzbetrieb - Ein Ansatz zur Koordinierung von Netzbetriebinstanzen verschiedener Netzebenen, Ilmenau, Germany: Universitätsverlag Ilmenau, 2017.
- [56] D. Westermann, M. Wolter, P. Komarnicki, S. Schlegel, R. Schwerdfeger, A. Richter and B. Arendarski, "Control Strategies for a Fully RES Based Power System," in *International ETG Congress 2017*, Bonn, Germany, Nov. 2017.
- [57] O. Pohl, F. Rewald, S. Dalhues, P. Jörke, C. Rehtanz, C. Wietfeld, A. Kubis, R. Kentchim and D. Kirsten, "Advancements in Distributed Power Flow Control," in *2018 53rd International Universities Power Engineering Conference (UPEC)*, Glasgow, UK, Sep. 2018.
- [58] A. Hermann, PhD Thesis: Market-Based Methods For The Coordinated Use Of Distributed Energy Resources - TSO-DSO Coordination in Liberalized Power Systems, Kongens Lyngby, Denmark: Technical University of Denmark, 2019.
- [59] E. Diskin, P. Cuffe and A. Keane, "Distribution System Reactive Power Management Under Defined Power Transfer Standards," in *IEEE PES General Meeting*, Vancouver, BC, Canada, Jul. 2013.
- [60] J. R. de Silva, C. P. Arnold and J. Arrillaga, "Capability Chart for an HVDC Link," *IEE Proceedings*, vol. 134C, no. 3, pp. 181-186, May 1987.
- [61] N. E. Nilsson and J. Mercurio, "Synchronous Generator Capability Curve Testing and Evaluation," *IEEE Transactions on Power Delivery*, vol. 9, no. 1, pp. 414-424, Jan. 1994.
- [62] A. Losi, M. Russo, P. Verde and D. Menniti, "Capability Chart for Generator-transformer Units," in *MELECON*, Bari, Italy, Aug. 1996.
- [63] G. Gargiulo, V. Mangoni and M. Russo, "Capability Charts for Combined Cycle Power Plants," *IEE Proceedings Generation Transmission Distribution*, vol. 149, no. 4, pp. 407-415, Jul 2002.

- [64] A. M. Noman, A. A. Al-Shamma'a, K. E. Addoweesh, A. A. Alabduljabbar and A. I. Alolah, "Simulation and Comparison of Three Phase CHB MLI and Three Phase Cascaded Voltage Source MLI Topologies for Grid Connected PV Applications," in *IECON 2017*, Beijing, China, Nov. 2017.
- [65] G. Ertasgin, D. Whaley, N. Ertugrul and W. L. Soong, "A Current-Source Grid-Connected Converter Topology for Photovoltaic Systems," in *AUPEC 2006*, Melbourne, Australia, Dec. 2006.
- [66] E. Enrique, "Use of Capability Curves for the Analysis of Reactive Power Compensation in Solar Farms," in *I&CPS 2017*, Niagara Falls, ON, Canada, May 2017.
- [67] R. Albarracín and M. Alonso, "Photovoltaic Reactive Power Limits," in *International Conference on Environment and Electrical Engineering*, Wroclaw, Poland, May 2013.
- [68] A. Cabrera-Tobar, E. Bullich-Massagué, M. Aragües-Peñalba and O. Gomis-Bellmunt, "Reactive Power Capability Analysis of a Photovoltaic Generator for Large Scale Power Plants," in *IET RPG 2016*, London, UK, Sep. 2016.
- [69] F. Delfino, R. Procopio, M. Rossi and G. Ronda, "Integration of Large-Size Photovoltaic Systems into the Distribution Grids: a P–Q Chart Approach to Assess Reactive Support Capability," *IET Renewable Power Generation*, vol. 4, no. 4, pp. 329-340, 2010.
- [70] A. Ellis, R. Nelson, E. Von Engeln, R. Walling, J. MacDowell, L. Casey, E. Seymour, W. Peter, C. Barker, B. Kirby and J. R. Williams, "Reactive Power Performance Requirements for Wind and Solar Plants," in *IEEE PES General Meeting*, San Diego, USA, 2012.
- [71] M. Ivas, A. Marušić, J. G. Havelka and I. Kuzle, "P-Q Capability Chart Analysis of Multi-inverter Photovoltaic Power Plant," *Electrical Power and Energy Systems*, vol. 116, 2020.
- [72] T. Ackermann, *Wind Power in Power Systems*, Stockholm, Sweden: John Wiley & Sons, Ltd., 2005.
- [73] IEC, *IEC 61400-27-1 Electrical Simulation Models - Wind Turbines*, Geneva, Switzerland: IEC, 2015.

- [74] M. E. Montilla-DJesus, S. Arnaltes, E. D. Castronuovo and D. Santos-Martin, "Optimal Power Transmission of Offshore Wind Power Using a VSC-HVDC Interconnection," *Energies*, vol. 10, no. 1046, pp. 1-16, 2017.
- [75] A. P. Tennakoon, J. B. Ekanayake, A. Atputharajah and S. G. Abeyratne, "Capability Chart of a Doubly Fed Induction Generation Based on its Ratings and Stability Margin," in *International Universities Power Engineering Conference (UPEC)*, Cardiff, UK, Sep. 2010.
- [76] J. Tian, C. Su and Z. Chen, "Reactive Power Capability of the Wind Turbine with Doubly Fed Induction Generator," in *IECON 2013*, Vienna, Austria, Nov. 2013.
- [77] T. Lund, P. Sørensen and J. Eek, "Reactive Power Capability of a Wind Turbine with Doubly Fed Induction Generator," *Wind Energy*, vol. 10, pp. 379-394, 2007.
- [78] M. El Achkar, R. Mbayed, G. Salloum, S. Le Ballois and E. Monmasson, "Generic Study of the Power Capability of a Cascaded Doubly Fed Induction Machine," *Electrical Power and Energy Systems*, vol. 86, pp. 61-70, 2017.
- [79] L. Meegahapola, T. Littler and S. Perera, "Capability Curve Based Enhanced Reactive Power Control Strategy for Stability Enhancement and Network Voltage Management," *Electrical Power and Energy Systems*, vol. 52, pp. 96-106, 2013.
- [80] I. Erlich, M. Wilch and C. Feltes, "Reactive Power Generation by DFIG Based Wind Farms with AC Grid Connection," in *IEEE Powertech*, Lausanne, Switzerland, 2008.
- [81] J. A. Martin and I. A. Hiskens, "Reactive Power Limitation due to Wind-Farm Collector Networks," in *IEEE Powertech*, Eindhoven, Netherlands, Jul. 2015.
- [82] M. Sarkar, M. Altin, P. E. Sørensen and A. D. Hansen, "Reactive Power Capability Model of Wind Power Plant Using Aggregated Wind Power Collection System," *Energies*, vol. 12, no. 1607, pp. 1-19, 2019.
- [83] N. R. Ullah, K. Bhattacharya and T. Thiringer, "Wind Farms as Reactive Power Ancillary Service Providers—Technical and Economic Issues," *IEEE Transactions on Energy Conversion*, vol. 24, no. 3, pp. 661-672, Sep. 2009.

- [84] A. Ríos, S. Arnaltes and J. L. Rodríguez-Amenedo, "Reactive Capability Limits of Wind Farms," *Int. J. Energy Technology and Policy*, vol. 3, no. 3, pp. 213-222, 2005.
- [85] E. Enrique, "Generation Capability Curves for Wind Farms," in *SusTech 2014*, Portland, OR, USA, Jul. 2014.
- [86] M. H. Hassam, D. Helmi, M. Elshahed and H. Abd-Elkhalek, "Improving the Capability Curves of a Grid-Connected Wind Farm: Gabel El-Zeit, Egypt," in *MEPCON 2017*, Menoufia, Egypt, Dec. 2017.
- [87] S. Mondal and D. Kastha, "Maximum Active and Reactive Power Capability of a Matrix Converter-Fed DFIG-Based Wind Energy Conversion System," *IEEE Journal of Emerging and Selected Topics in Power Electronics*, vol. 5, no. 3, pp. 1322-1333, 2017.
- [88] P. Cuffe, P. Smith and A. Keane, "Transmission System Impact of Wind Energy Harvesting Networks," *IEEE Transactions on Sustainable Energy*, vol. 3, no. 4, pp. 643-651, Oct. 2012.
- [89] S. Engelhardt, I. Erlich, C. Feltes, J. Kretschmann and F. Shewarega, "Reactive Power Capability of Wind Turbines Based on Doubly Fed Induction Generators," *IEEE Transactions on Energy Conversion*, vol. 26, no. 1, pp. 364-372, Mar. 2011.
- [90] N. Dinic, B. Fox, D. Flynn, L. Xu and A. Kennedy, "Increasing Wind Farm Capacity," *IEE Proc.-Gener. Transm. Distrib.*, vol. 153, no. 4, pp. 493-498, 2006.
- [91] M. Džamarija, M. Bakhtvar and A. Keane, "Operational Characteristics of Non-firm Wind Generation in Distribution Networks," in *IEEE PES General Meeting*, San Diego, CA, USA, Jul. 2012.
- [92] O. Krishan and S. Suhag, "An Updated Review of Energy Storage Systems: Classification and Applications in Distributed Generation Power Systems Incorporating Renewable Energy Resources," *International Journal of Energy Research*, vol. 43, pp. 6171-6210, 2019.
- [93] D. O. Akinyele and R. K. Rayudu, "Review of Energy Storage Technologies for Sustainable Power Networks," *Sustainable Energy Technologies and Assessments*, vol. 8, pp. 74-91, 2014.

- [94] L. Chang, W. Zhang, S. Xu and K. Spence, "Review on Distributed Energy Storage Systems for Utility Applications," *CPSS Transactions on Power Electronics and Applications*, vol. 2, no. 4, pp. 267-276, Dec. 2017.
- [95] N. W. Miller, R. S. Zrebiec, R. W. Delmerico and G. Hunt, "Design and Commissioning of a 5MVA, 2.5 MWH Battery Energy Storage System," in *IEEE T&D Conference and Exposition*, Los Angeles, CA, USA, Sep. 1996.
- [96] A. Gabash and P. Li, "Evaluation of Reactive Power Capability by Optimal Control of Wind-Vanadium Redox Battery Stations in Electricity Market," in *International Conference on Renewable Energies and Power Quality (ICREPQ)*, Las Palmas de Gran Canaria, Spain, Apr. 2011.
- [97] S. Kundu, K. Kalsi and S. Backhaus, "Approximating Flexibility in Distributed Energy Resources: A Geometric Approach," in *Power Systems Computing Conference (PSCC)*, Dublin, Ireland, Jun. 2018.
- [98] G. K. Irungu, A. O. Akumu and D. K. Murage, "Modeling Industrial Load Due to Severe Voltage Surges and Sags: 'A Case Study of Magadi Soda Company'," in *AFRICON*, Windhoek, South Africa, 2007.
- [99] C. Sourkounis and P. Tourou, "Grid Code Requirements for Wind Power Integration in Europe," in *Power Options for the Eastern Mediterranean Region (POEM)*, Limassol, Cyprus, Nov. 2012.
- [100] N. I. Sarkar, L. G. Meegahapola and M. Datta, "Reactive Power Management in Renewable Rich Power Grids: A Review of Grid-Codes, Renewable Generators, Support Devices, Control Strategies and Optimization Algorithms," *IEEE Access*, vol. 6, pp. 41458-41489, May 2018.
- [101] A. Ellis, R. Nelson, E. Von Engel, R. Walling, J. MacDowell, L. Casey, E. Seymour, W. Peter, C. Barker, B. Kirby and J. R. Williams, "Review of Existing Reactive Power Requirements for Variable Generation," in *IEEE PES General Meeting*, San Diego, CA, USA, Jul. 2012.
- [102] IEEE, "1547-2018 - IEEE Standard for Interconnection and Interoperability of Distributed Energy Resources with Associated Electric Power Systems Interfaces," IEEE, 2018.
- [103] M. Rossi, G. Vigano, D. Moneta, M. T. Vespucci and P. Pisciella, "Fast Estimation of Equivalent Capability for Active Distribution Networks," in *CIREN*, Glasgow, Scotland, Jun. 2017.

- [104] M. Sarstedt, L. Kluß, J. Gerster, T. Meldau und L. Hofmann, „Survey and Comparison of Optimization-Based Aggregation Methods for the Determination of the Flexibility Potentials at Vertical System Interconnections,“ *Energies*, Bd. 14, Nr. 687, Jan. 2021.
- [105] A. Losi, F. Rossi, M. Russo and P. Verde, "Capability Chart for the Planning of Reactive Power Resources," in *MELECON*, Bari, Italy, May 1996.
- [106] Z. Tan, H. Zhong, Q. Xia, C. Kang, X. Wang and H. Tang, "Estimating the Robust P-Q Capability of a Technical Virtual Power Plant under Uncertainties," *IEEE Transactions on Power Systems*, vol. 35, no. 6, pp. 4285-4296, Nov. 2020.
- [107] CAISO, "What the Duck Curve Tells us About Managing a Green Grid," CAISO, Folsom, CA, USA, 2016.
- [108] D. A. Contreras and K. Rudion, "Computing the feasible operating region of active distribution networks: Comparison and validation of random sampling and optimal power flow based methods," *IET Generation, Transmission & Distribution*, vol. 15, no. 10, pp. 1600-1612, Jan. May 2021.
- [109] E. Handschin, C. Rehtanz, H. F. Wedde, O. Krause and S. Lehnhoff, "On-Line Stable State Determination in Decentralized Power Grid Management," in *Power Systems Computation Conference (PSCC)*, Glasgow, Scotland, Jul. 2008.
- [110] O. Krause, S. Lehnhoff, E. Handschin, C. Retanz and H. F. Wedde, "On Feasibility Boundaries of Electrical Power Grids in Steady State," *Electrical Power and Energy Systems*, vol. 31, pp. 437-444, 2009.
- [111] R. Schneider, *Convex bodies: the Brunn–Minkowski theory*, Cambridge, UK: Cambridge University Press, 2013.
- [112] S. Das und S. Sarvottamananda, „Computing the Minkowski Sum of Convex Polytopes in \mathbb{R}^d ,“ Nov. 2018.
- [113] A. Bernstein, J.-Y. Le Boudec, M. Paolone, L. Reyes-Chamorro and W. Saab, "Aggregation of Power Capabilities of Heterogeneous Resources for Real-Time Control of Power Grids," in *Power Systems Computation Conference (PSCC)*, Genoa, Italy, Jun. 2016.
- [114] L. Zhao, W. Zhang, H. Hao and K. Kalsi, "A Geometric Approach to Aggregate Flexibility Modeling of Thermostatically Controlled Loads," *IEEE Transactions on Power Systems*, vol. 32, no. 6, pp. 4721-4731, Nov. 2017.

- [115] M. S. Nazir, I. A. Hiskens, A. Bernstein and E. Dall'Anese, "Inner Approximation of Minkowski Sums: A Union-Based Approach and Applications to Aggregated Energy Resources," in *IEEE Conference on Decision and Control (CDC)*, Miami Beach, FL, USA, Dec. 2018.
- [116] P. Bailly, A. Michiorri and G. Kariniotakis, "Recursive Estimation of Flexibilities in a Radial Distribution Network," in *CIREN*, Madrid, Spain, Jun. 2019.
- [117] Z. Yang, H. Zhong, Q. Xia, A. Bose and C. Kang, "Optimal Power Flow Based on Successive Linear Approximation of Power Flow Equations," *IET Generation Transmission Distribution*, vol. 10, no. 14, pp. 3654-3662, 2016.
- [118] L. Ageeva, M. Majidi and D. Pozo, "Analysis of Feasibility Region of Active Distribution Networks," in *2019 International Youth Conference on Radio Electronics, Electrical and Power Engineering (REEPE)*, Moscow, Russia, Mar. 2019.
- [119] D. A. Contreras and K. Rudion, "Verification of Linear Flexibility Range Assessment in Distribution Grids," in *Powertech 2019*, Milan, Italy, Jun. 2019.
- [120] C. Phillips, J. Anderson, G. Huber and S. Glotzer, "Optimal Filling of Shapes," *Physical Review Letters*, vol. 108, 2012.
- [121] H. Blum, *A Transformation for Extracting New Descriptors of Shape*, MIT Press, 1967, pp. 362-380.
- [122] F. Capitanescu, "Critical Review of Recent Advances and Developments Needed in AC Optimal Power Flow," *Electric Power Systems Research*, vol. 136, pp. 57-68, 2016.
- [123] A. V. Jayawardena, L. G. Meegahapola, D. A. Robinson and S. Perera, "Microgrid Capability Diagram: A Tool for Optimal Grid-tied Operation," *Renewable Energy*, vol. 74, pp. 497-504, 2015.
- [124] H. Chen and A. Moser, "Improved Flexibility of Active Distribution Grid by Remote Control of Renewable Energy Sources," in *International Conference on Clean Electrical Power*, Liguria, Italy, 2017.
- [125] F. Capitanescu, "TSO-DSO Interaction: Active Distribution Network Power Chart for TSO Ancillary Services Provision," *Electric Power*, vol. 163, pp. 226-230, Oct. 2018.

- [126] J. Buire, F. Colas, J.-Y. Dielout and X. Guillaud, "Stochastic Optimization of PQ Powers at the Interface between Distribution and Transmission Grids," *Energies*, vol. 12, pp. 1-16, Oct. 2019.
- [127] M. Kalantar-Neyestanaki, F. Sossan, M. Bozorg and R. Cherkaoui, "Characterizing the Reserve Provision Capability Area of Active Distribution Networks: A Linear Robust Optimization Method," *IEEE Transactions on Smart Grid*, vol. 11, no. 3, pp. 2464-2475, May 2020.
- [128] S. Bolognani and S. Zampieri, "On the Existence and Linear Approximation of the Power Flow Solution in Power Distribution Networks," *IEEE Transactions on Power Systems*, vol. 31, no. 1, pp. 163-172, 2016.
- [129] G. Valverde and J. J. Orozco, "Reactive Power Limits in Distributed Generators from Generic Capability Curves," in *IEEE PES General Meeting*, National Harbor, MD, USA, 2014.
- [130] S. Bolognani und F. Dörfler, „Fast Power System Analysis via Implicit Linearization of the Power Flow Manifold,“ in *Fifty-third Annual Allerton Conference*, Allerton House, UIUC, Illinois, USA, Sep. 2015.
- [131] D. Lee, H. Nguyen, K. Dvijotham and K. Turitsyn, "Convex Restriction of Power Flow Feasibility Sets," *IEEE Transactions on Control of Network Systems*, vol. 6, no. 3, pp. 1235-1245, Sep. 2019.
- [132] Z. Yang, H. Zhong, A. Bose, T. Zheng, Q. Xia and C. Kang, "A Linearized OPF Model With Reactive Power and Voltage Magnitude: A Pathway to Improve the MW-Only DC OPF," *IEEE Transactions on Power Systems*, vol. 33, no. 2, pp. 1734-1745, Mar. 2018.
- [133] D. Wang, K. Turitsyn and M. Chertkov, "DistFlow ODE: Modeling, Analyzing and Controlling Long Distribution Feeder," in *51st IEEE Conference on Decision and Control*, Maui, HI, USA, Dec. 2012.
- [134] Verband der Elektrotechnik Elektronik Informationstechnik e.V. (VDE), "Power Generation Systems Connected to the Low-voltage Distribution," VDE-AR-N 4105:2011-08, Aug. 2011.
- [135] H. Kim and W. Kim, "Integrated Optimization of Combined Generation and Transmission Expansion Planning Considering Bus Voltage Limits," *Journal of Electrical Engineering and Technology*, vol. 9, no. 4, pp. 1202-1209, Jul. 2014.

- [136] P. Pareek and A. Verma, "Linear OPF with Linearization of Quadratic Branch Flow Limits," in *2018 IEEMA Engineer Infinite Conference (eTechNxT)*, New Delhi, India, Mar. 2018.
- [137] K. Volk, L. Rupp, K. Geschermann and C. Lakenbrink, "Managing Local Flexible Generation and Consumption Units Using a Quota-Based Grid Traffic Light Approach," in *CIREC*, Madrid, Spain, Jun. 2019.
- [138] R. de Groot, J. Morren and J. Slootweg, "Investigation of Grid Loss Reduction und Closed-Ring Operation of MV Distribution Grids," in *IEEE PES General Meeting*, Ann Harbor, MD, USA, Jul. 2014.
- [139] J. McDonald, B. Wojszczyk, B. Flynn and I. Voloh, "Distribution Systems, Substations, and Integration of Distributed Generation," in *Electrical Transmission Systems and Smart Grids*, New York, NY, USA, Springer, 2013, pp. 7-68.
- [140] D. A. Contreras and K. Rudion, "Impact of Grid Topology and Tap Position Changes on the Flexibility Provision from Distribution Grids," in *ISGT Europe*, Bucharest, Romania, Oct. 2019.
- [141] D. A. Contreras and K. Rudion, "Time-Based Aggregation of Flexibility at the TSO-DSO Interconnection Point," in *IEEE PES General Meeting*, Atlanta, GA, USA, Aug. 2019.
- [142] E. Polymeneas and S. Meliopoulos, "Aggregate Modeling of Distribution Systems for Multi-Period OPF," in *Power Systems Computation Conference (PSCC)*, Genoa, Italy, Jun. 2016.
- [143] K. Rudion, A. Orths, Z. A. Styczynski and K. Strunz, "Design of Benchmark of Medium Voltage Distribution Network for Investigation of DG Integration," in *IEEE Power Engineering Society General Meeting*, Montreal, Que., Canada, Jun. 2006.
- [144] CIGRE, "Benchmark Systems for Network Integration of Renewable and Distributed Energy Resources," CIGRE Task force C6.04.02, 2011.
- [145] M. Brunner, PhD Thesis: Auswirkungen von Power-to-Heat in elektrischen Verteilnetzen, Stuttgart, Germany: Universität Stuttgart, 2017.
- [146] M. Kraiczy, G. Lammert, T. Stetz, S. Gehler, G. Arnold, M. Braun, S. Schmidt, H. Homeyer, U. Zickler, F. Sommerwerk and C. Elbs, "Parameterization of Reactive Power Characteristics for Distributed

- Generators: Field Experience and Recommendations," in *ETG Congress 2015*, Bonn, Germany, Nov. 2015.
- [147] B. Gorgan, S. Busoi, G. Tanasescu and P. V. Nothinger, "PV Plant Modeling for Power System Integration Using PSCAD Software," in *International Symposium on Advanced Topics in Electrical Engineering*, Bucharest, Romania, May 2015.
- [148] M. Legry, J.-Y. Dieulot, F. Colas, C. Saudemont and O. Ducarne, "Non-linear Primary Control Mapping for Droop-like Behavior of Microgrid Systems," *IEEE Transactions on Smart Grid*, 2020.
- [149] R. Schwerdfeger, S. Schlegel, D. Werstermann, M. Lutter and M. Junghans, "Methodology for Next Generation System Operation Between DSO and DSO," in *CIGRE Session*, Paris, France, 2016.
- [150] M. Banka, D. Contreras and K. Rudion, "Multi-Agent Based Strategy for Controlled Islanding and System Restoration Employing Dispersed Generation," in *CIGRE Workshop*, Berlin, Germany, 2020.
- [151] R. Schwerdfeger, S. Schlegel and D. Westermann, "Approach for N-1 Secure Grid Operation with 100% Renewables," in *IEEE PES General Meeting*, Boston, USA, Jul. 2016.
- [152] H. Wang, S. Riaz and P. Mancarella, "Integrated Techno-Economic Modeling, Flexibility Analysis, and Business Case," *Applied Energy*, vol. 259, no. 1, 2020.
- [153] P. Wiest, D. Gross, K. Rudion and A. Probst, "Rapid Identification of Worst-Case Conditions: Improved Planning of Active Distribution Grids," *IET Generation, Transmission & Distribution*, vol. 11, no. 9, pp. 2412-2417, 2017.
- [154] P. Wiest, D. Contreras, D. Groß and K. Rudion, "Synthetic Load Profiles of Various Customer Types for Smart Grid Simulations," in *NEIS Conference*, Hamburg, Germany, 2018.
- [155] J. Merino, J. E. Rodriguez-Seco, C. Caerts, K. Visscher, R. D'hulst, E. Rikos and A. Temiz, "Scenarios and Requirements for the Operation of the 2030+ Electricity Network," in *CIGRE*, Lyon, France, Jun. 2015.
- [156] F. Marten, L. Löwer, J. C. Töbermann and M. Braun, "Optimizing the Reactive Power Balance Between a Distribution and Transmission Grid

- Through Iteratively Updated Grid Equivalents," in *Power Systems Computing Conference (PSCC)*, Wroclaw, Poland, Feb. 2015.
- [157] F. Capitanescu, "OPF Integrating Distribution Systems Flexibility for TSO Real-Time Active Power Balance Management," in *MEDPOWER 2018*, Cavtat, Croatia, Nov. 2018.
- [158] F. Rewald, O. Pohl and C. Rehtanz, "State Estimation and Determination of Flexibility Potential in Medium Voltage Networks," in *International Workshop on Flexibility and Resiliency Problems of Electric Power Systems (FREPS 2019)*, Irkutsk, Russia, Aug. 2019.
- [159] R. D. Zimmerman, C. E. Murrillo-Sanchez and R. J. Thomas, "MATPOWER: Steady-State Operations, Planning and Analysis Tools for Power Systems Research and Education," *IEEE Transactions on Power Systems*, vol. 26, no. 1, pp. 12-19, Feb. 2011.